

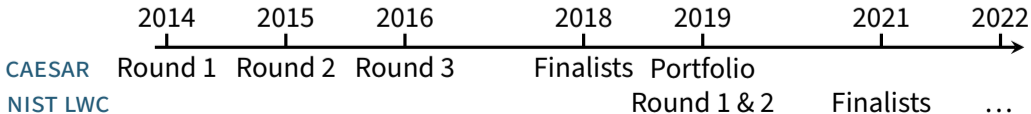
# Update on the Security Analysis of ASCON

Christoph Dobraunig   **Maria Eichlseder**   Johannes Erlacher   Florian Mendel   Martin Schläffer

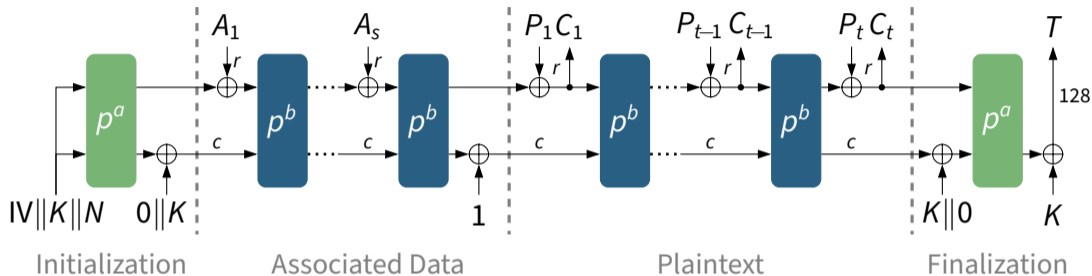
NIST LWC Workshop 2022 – 11 May 2022

# The ASCON Family

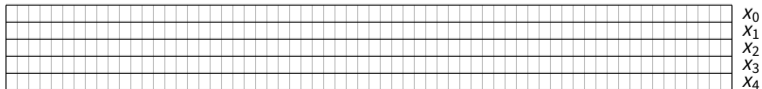
- ✍ Designed in 2014 [DEMS16]
- 🏆 Selected in CAESAR portfolio as first choice for lightweight AEAD in 2019
- 📖 Published in Journal of Cryptology in 2021 [DEMS21c]
- 🔍 Extensive published third-party cryptanalysis confirming its security margin
- ★ **This talk:** Overview of recent third-party cryptanalysis results & our own work on new security bounds [EME22]



# ASCON's Mode for Authenticated Encryption

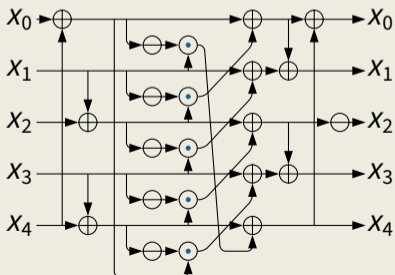
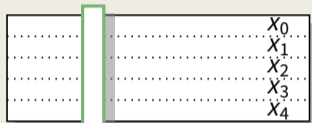


- **Doubly-keyed** initialization/finalization for higher robustness under misuse
- **Duplex sponge** mode using a  $5 \times 64 = 320$ -bit permutation

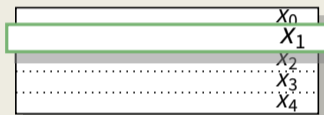


# ASCON Permutation: $a = 12$ , $b \in \{6, 8\}$ Rounds

## S-box layer



## Linear layer



$$X'_0 := X_0 \oplus (X_0 \ggg 19) \oplus (X_0 \ggg 28)$$

$$X'_1 := X_1 \oplus (X_1 \ggg 61) \oplus (X_1 \ggg 39)$$

$$X'_2 := X_2 \oplus (X_2 \ggg 1) \oplus (X_2 \ggg 6)$$

$$X'_3 := X_3 \oplus (X_3 \ggg 10) \oplus (X_3 \ggg 17)$$

$$X'_4 := X_4 \oplus (X_4 \ggg 7) \oplus (X_4 \ggg 41)$$

# Analysis of ASCON

Key recovery	ASCON initialization	7 / 12	$2^{97}$		Cube-like	[LZWW17]
	ASCON initialization	7 / 12	$2^{104}$		Cube-like	[LDW17]
	ASCON initialization	7 / 12	$2^{123}$		Cube	[RHSS21]
	ASCON initialization	6 / 12	$2^{74}$		Cond. HDL	[HP22]
	ASCON initialization	5 / 12	$2^{31}$		Diff.-linear	[Tez20]
	ASCON-128a iteration	7 / 8	$2^{118}$		Cond. cube	[CKT22]
	ASCON-80pq iteration	6 / 6	$2^{130}$		Cond. cube	[CHK22]
Forgery	ASCON-128 finalization	6 / 12	$2^{33}$		Cube tester	[LZWW17]
	ASCON-128 finalization	4 / 12	$2^{102}$		Differential	[DEMS15]
	ASCON-128 finalization	4 / 12	$2^{97}$		Differential	[GPT21]
	ASCON-128a finalization	3 / 12	$2^{20}$		Differential	[GPT21]

= nonce misuse   
 = exceeds data limit of  $2^{64}$  blocks   
 = time exceeds  $2^{128}$   
 weak-key variants omitted

# Analysis of ASCON: (Partial\*) state recovery


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State recovery	ASCON-128 iteration	6 / 6	$2^{40}$	🚫	Cond. cube	[BCP22]
	ASCON-128 iteration*	6 / 6	$2^{45}$	🚫	Cond. cube	[CHK22]
	ASCON-128 iteration	5 / 6	$2^{66}$	🚫	Cube-like	[LZWW17]
	ASCON-128a iteration	7 / 8	$2^{118}$	🚫🚫	Cond. cube	[CKT22]
	ASCON-128a iteration	3 / 8	$2^{117}$	✅	Differential	[GPT21]
	ASCON-128a iteration	2 / 8	—	✅	Sat-Solver	[DKM+17]

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🚫 = nonce misuse    🚫 = exceeds data limit of  $2^{64}$  blocks  
weak-key variants omitted




# Analysis of ASCON-HASH and ASCON-XOF

Type	Target	Output size	Rounds	Time	Method	Reference
Preimage	ASCON-XOF	64	6 / 12	$2^{63.3}$	Algebraic	[DEMS19]
	ASCON-XOF	64	2 / 12	$2^{39}$	Cube-like	[DEMS19]
Collision	ASCON-XOF	all	4 / 12	– 	Differential	[DEMS19]
	ASCON-XOF	64	2 / 12	$2^{15}$	Differential	[ZDW19]
	ASCON-HASH	256	2 / 12	$2^{125}$	Differential	[ZDW19]
	ASCON-HASH	256	2 / 12	$2^{103}$	Differential	[GPT21]


( = chosen IV)

# Analysis of ASCON's Permutation

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Distinguisher	Permutation	12 / 12	$2^{55}$ 	Zero-sum	[HP22]
	Permutation	11 / 12	$2^{85}$ 	Zero-sum	[DEMS21a]
	Permutation	8 / 12	$2^{46}$	Integral	[HP22]
	Permutation	7 / 12	$2^{65}$	Integral	[Tod15]
	Permutation	7 / 12	$2^{60}$	Integral	[RHSS21]
	Permutation	7 / 12	$2^{34}$ 	Limited-Birthday	[GPT21]
	Permutation	5 / 12	$2^{109}$	Truncated Differential	[Tez16]
	Permutation	5 / 12	$2^{80}$	Rectangle	[GPT21]
	Permutation	5 / 12	-	Zero-Correlation	[DEMS21a]
	Permutation	5 / 12	-	Impossible Differential	[DEMS21a]
	Permutation	4 / 12	$2^{107}$	Differential	[DEMS21a]
	Permutation	4 / 12	$2^{101}$	Linear	[DEM15a]
	Permutation	3 / 12	-	Subspace Trails	[LTW18]

---

( = non-black-box distinguisher)



# Analysis of Round-Reduced ASCON



Recent third-party analysis

# Improvements to 7-Round Cube Attacks

## Misuse-Free Key-Recovery and Distinguishing Attacks on 7-Round Ascon


Raghvendra Rohit<sup>1</sup>, Kai Hu<sup>2,5</sup>, Sumanta Sarkar<sup>3</sup> and Siwei Sun<sup>4,6</sup>


<sup>1</sup> Univ Rennes, Centre National de la Recherche Scientifique (CNRS), Institut de Recherche en

## Diving Deep into the Weak Keys of Round Reduced Ascon

Raghvendra Rohit<sup>1</sup> and Santanu Sarkar<sup>2,3</sup>

<sup>1</sup> Cryptography Research Centre, Technology Innovation Institute, Abu Dhabi, UAE

 [RHSS21] slightly reduced the data complexity of 7-round attacks to stay **below the limit of  $2^{64}$  blocks**.

 [RS21] investigated classes of “**weak keys**” which permit slightly better cube attacks for 7 rounds.

# Refined Results for Differential Attacks


## Exploring Differential-Based Distinguishers and Forgeries for ASCON


David Gerault<sup>1,2</sup>, Thomas Peyrin<sup>1</sup> and Quan Quan Tan<sup>1</sup>

<sup>1</sup> Nanyang Technological University, Singapore, Singapore

## Towards Tight Differential Bounds of Ascon

IACR FSE Rump Session 2022

 [GPT21] investigate the applicability of **differential distinguishers for forgeries and collisions**.


 [MR22] find characteristics with **fewer active S-boxes** for 4 rounds (44  $\rightarrow$  43) and 5 rounds (78  $\rightarrow$  72).

# (Higher-Order) Differential-Linear Distinguishers

## Differential-linear Attacks on Permutation Ciphers Revisited: Experiments on Ascon and DryGASCON


Ash Başak Civek<sup>a</sup> and Cihangir Tezcan<sup>b</sup>

*tics Institute, Department of Cyber Security, CyDeS Laboratory, Middle East Technical University, Ankara*

 [CT22] provide experiments on **differential-linear cryptanalysis** to refine previous results on 7 rounds.

## Revisiting Higher-Order Differential(-Linear) Attacks from an Algebraic Perspective Applications to ASCON, GRAIN v1, Xoodoo, and ChaCha

Kai Hu and Thomas Peyrin


 [HP22] investigate **higher-order DL distinguishers** and find 8-round permutation distinguishers in a dedicated setting and 6-round key-recovery attacks.

# Other Distinguishers

## Simplified MITM Modeling for Permutations: New (Quantum) Attacks

André Schrottenloher and Marc Stevens


Cryptology Group, CWI, Amsterdam, The Netherlands  
firstname.lastname@cwi.nl

 [SS22a; SS22b] show that **structural MitM attacks** can find a fixpoint  $x = P(x)$  for up to 2.5 rounds with complexity  $2^{272}$ .

## Exploring Differential-Based Distinguishers and Forgeries for ASCON

David Gerault<sup>1,2</sup>, Thomas Peyrin<sup>1</sup> and Quan Quan Tan<sup>1</sup>

<sup>1</sup> Nanyang Technological University, Singapore, Singapore

 [GPT21] find **limited-birthday distinguishers** up to 7 rounds.

# Misuse Analysis of ASCON



Recent third-party analysis

# Analysis of ASCON in Misuse Settings

- Cryptanalysis in standard settings has only lead to small improvements in the last years
- Cryptanalysts increasingly consider misuse settings:
  - Nonce misuse
  - Decryption misuse
  - Implementation attacks

# Analysis of Duplex Sponges in Misuse Settings

Generic nonce-misuse attacks on duplex designs include

- Confidentiality break  
with  $1 + 1$  misuse query per block of the challenge message.
- State recovery  
with  $D$  misuse queries,  $T \cdot D = 2^c$ .
  - Does not lead to trivial key recovery in ASCON

With more massive nonce misuse, some dedicated attacks are possible:




# Conditional Cube Attacks on ASCON in Misuse Settings

## Practical cube-attack against nonce-misused Ascon<sup>†</sup>


Jules Baudrin, Anne Canteaut and Léo Perrin

Inria, France

 [BCP22] find **conditional cube attacks** with nonce misuse for the full 6 encryption rounds of ASCON-128.


## ASCON-80pq in a Nonce-misuse Setting

Donghoon Chang<sup>1,2</sup>, Deukjo Hong<sup>1,3</sup>, and Jinkeon Kang<sup>1</sup>

 [CHK22] find similar results and KR attacks for ASCON-80pq ( $> 2^{128}$ ).

## A New Conditional Cube Attack on Reduced-Round Ascon-128a in a Nonce-misuse Setting

Donghoon Chang<sup>1,2</sup>, Jinkeon Kang<sup>1</sup> and Meltem Sönmez Turan<sup>1</sup>

 [CKT22] find **conditional cube attacks** with nonce misuse for 7 of 8 round in ASCON-128A and a key-recovery attack.

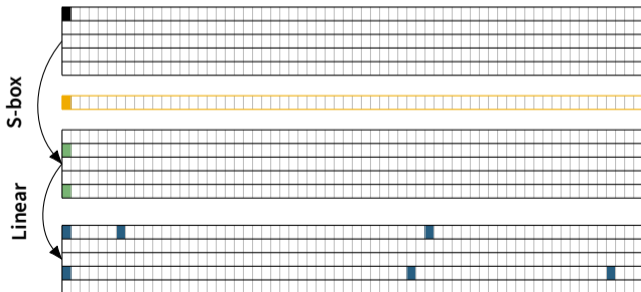
# Differential & Linear Cryptanalysis: New Bounds



ToSC 2022/1

# Differential and Linear Characteristics of ASCON

- **S-box** has max. differential probability  $2^{-2}$ , max. squared correlation  $2^{-2}$
- Goal: Prove lower bound on number of **active S-boxes** of characteristics
- **Weak alignment** → proving bounds is challenging, need bitwise model



# Bounds and Best Known Characteristics

Gap of **provable bounds** vs. **best known characteristics** [DEMS15; DEM15b; GPT21]:

	R	min #S-boxes		max Probability		Methods
Differential	1	1	1	$2^{-2}$	$2^{-2}$	DDT
	2	4	4	$2^{-8}$	$2^{-8}$	DDT
	3	15	15	$\leq 2^{-30}$	$2^{-40}$	SMT, nldtool
	4	-	44	-	$2^{-107}$	nldtool
	5	-	78	-	$2^{-190}$	CP
	6	-	-	-	-	

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	4	$\geq 36$	43	$\leq 2^{-72}$	$2^{-107}$	nldtool, SAT
	5	-	72	-	$2^{-190}$	CP, SAT
	6	$\geq 54$	-	$\leq 2^{-108}$	-	

➔ New lower bounds for **4** and **6** rounds [EME22]

➔ Slightly better characteristics [MR22]

# Bounds and Best Known Characteristics

Gap of **provable bounds** vs. **best known characteristics** [DEMS15; DEM15b; GPT21]:

	R	min #S-boxes		max Square Corr.	Methods	
Linear	1	1	1	$2^{-2}$	$2^{-2}$	LAT
	2	4	4	$2^{-8}$	$2^{-8}$	LAT
	3	13	13	$\leq 2^{-26}$	$2^{-28}$	SMT, lineartrails
	4	-	43	-	$2^{-98}$	lineartrails
	5	-	67	-	$2^{-186}$	lineartrails
	6	-	-	-	-	-

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# Approach for SAT Model to Prove Bounds

## Optimized SAT model

- ✓ SAT encoding for characteristics by Sun et al. [SWW21; SWW18]
- ✓ Different counter encodings



# Approach for SAT Model to Prove Bounds

## Optimized SAT model

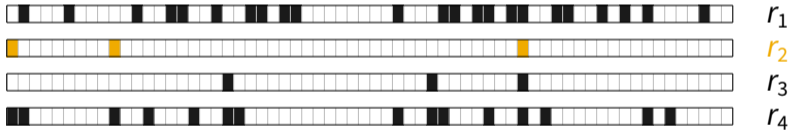
- ✓ SAT encoding for characteristics by Sun et al. [SWW21; SWW18]
- ✓ Different counter encodings

## Parallelization

- ✗ Solver-based [HKWB11; HFB20; BSS15; SS21]
- ✓ Manual partitioning

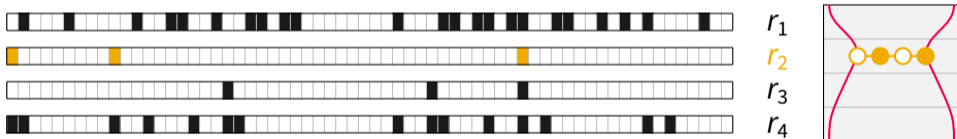
# Manual parallelization approach

- ➔ Partition the search space into **many independent problems**
- ➔ Categorize characteristics based on “**girdle patterns**”
  - S-box activity within the **round with fewest active S-boxes**



# Manual parallelization approach

- ➔ Partition the search space into **many independent problems**
- ➔ Categorize characteristics based on “**girdle patterns**”
  - S-box activity within the **round with fewest active S-boxes**

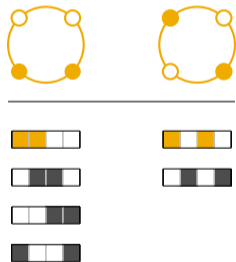


- ➔ Reduce the number of subproblems to be solved
- ➔ Optimize the individual SAT models

# Manual parallelization approach

## Consider **rotational symmetries**

- Use **necklace theory** to eliminate redundant checks [Mor72]



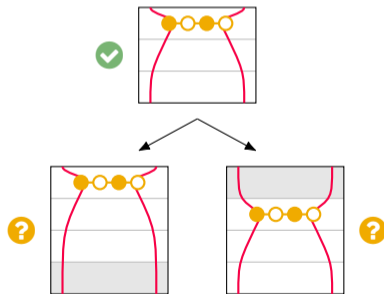
# Manual parallelization approach

## ↻ Consider **rotational symmetries**

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## ⚑ **Prefilter** individual problems

- Reduces model complexity



# Manual parallelization approach

## Consider **rotational symmetries**

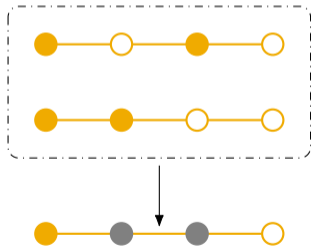
- Use **necklace theory** to eliminate redundant checks [Mor72]

## **Prefilter** individual problems

- Reduces model complexity

## **Pooling** individual problems

- Reduces overhead



# New Bounds

- Single characteristic for **4-round ASCON**
  - ➔  $\geq 36$  active S-boxes
  - ➔ Runtime  $\approx 600$  CPU days

## New Bounds

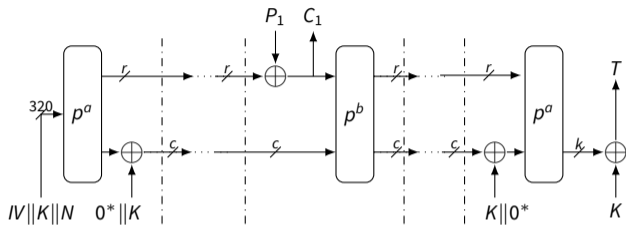
- Single characteristic for **4-round ASCON**
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- Single characteristic for **6-round ASCON**
  - ➔  $\geq 54$  active S-boxes
  - ➔ Runtime  $\approx 60$  CPU days
  - ➔ Utilizing intermediate results from our 4 round bound



# New Bounds

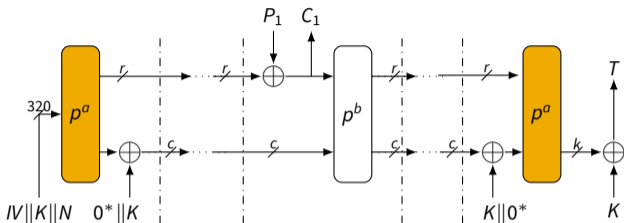
- Single characteristic for **4-round ASCON**
  - ➔  $\geq 36$  active S-boxes
  - ➔ Runtime  $\approx 600$  CPU days
- Single characteristic for **6-round ASCON**
  - ➔  $\geq 54$  active S-boxes
  - ➔ Runtime  $\approx 60$  CPU days
  - ➔ Utilizing intermediate results from our 4 round bound
- Almost certainly not tight, but good enough to support trust in the permutation

# Implications for ASCON



R	min #S	Probability
6	$\geq 54$	$\leq 2^{-108}$
8	$\geq 72$	$\leq 2^{-144}$
12	$\geq 108$	$\leq 2^{-216}$

## Implications for ASCON

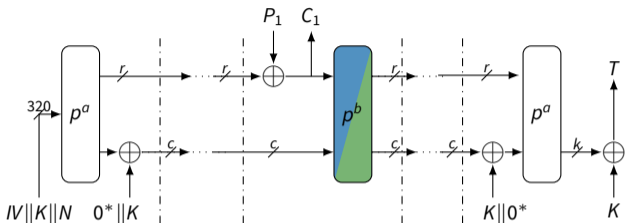


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### Authenticated Encryption: Initialization and Finalization

- **12 round** configuration
- Ample security margin for **128-bit security**

## Implications for ASCON

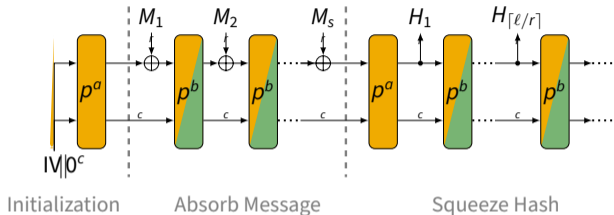


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### Authenticated Encryption: Data processing

- ASCON-128: **6 rounds**
- ASCON-128A: **8 rounds**
- Data limit of  $2^{64}$  encrypted blocks
- Goal: Find better (tighter) 6-round bound

## Implications for ASCON

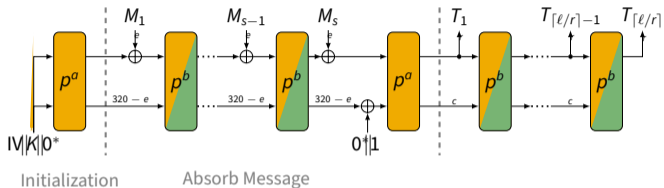


R	min #S	Probability
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### ASCON-HASH and ASCON-XOF

- Difficult to evaluate unkeyed modes based on probability
- Assumption:  $2^{-128}$  (attempts)  $\times 2^{-64}$  (degrees of freedom)
- ➔ **12 round** bound  $< 2^{-192}$

# Implications for ASCON

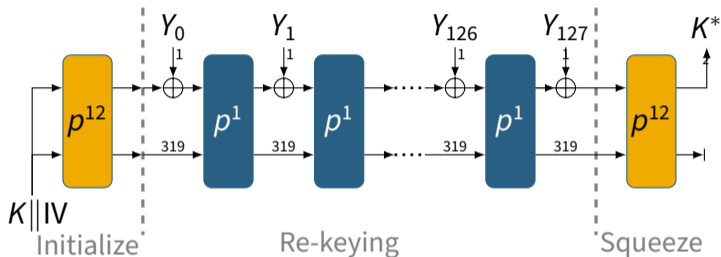


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## ASCON-MAC and ASCON-PRF [DEMS21b]

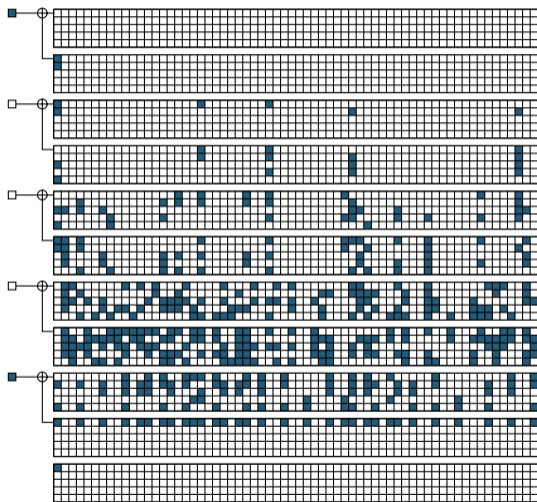
- ASCON-MAC, ASCON-PRF: **12 rounds**
- ASCON-MACA, ASCON-PRFA: **8 rounds**

## Bounds for ISAP



- **Scenario:** Create collision based on 1-bit absorption
- For **1 to 4** rounds (consecutive bits), **no solution exists**
- For **5** rounds, collision-producing characteristic with **105** active S-boxes exists
- General bound: For **3+** final rounds in any collision-producing characteristic with 1-bit rate, there are at least **64** active S-boxes

# Bounds for ISAP – 5-round characteristic





# Conclusion

- 📄 ASCON has received a lot of attention by cryptanalysts
  - during CAESAR and during NIST LWC
- 🔍 Main results: Optimizations of 7-round cube attack; Misuse attacks
- ✅ No cryptanalytic breakthroughs
- ✅ Improved bounds

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